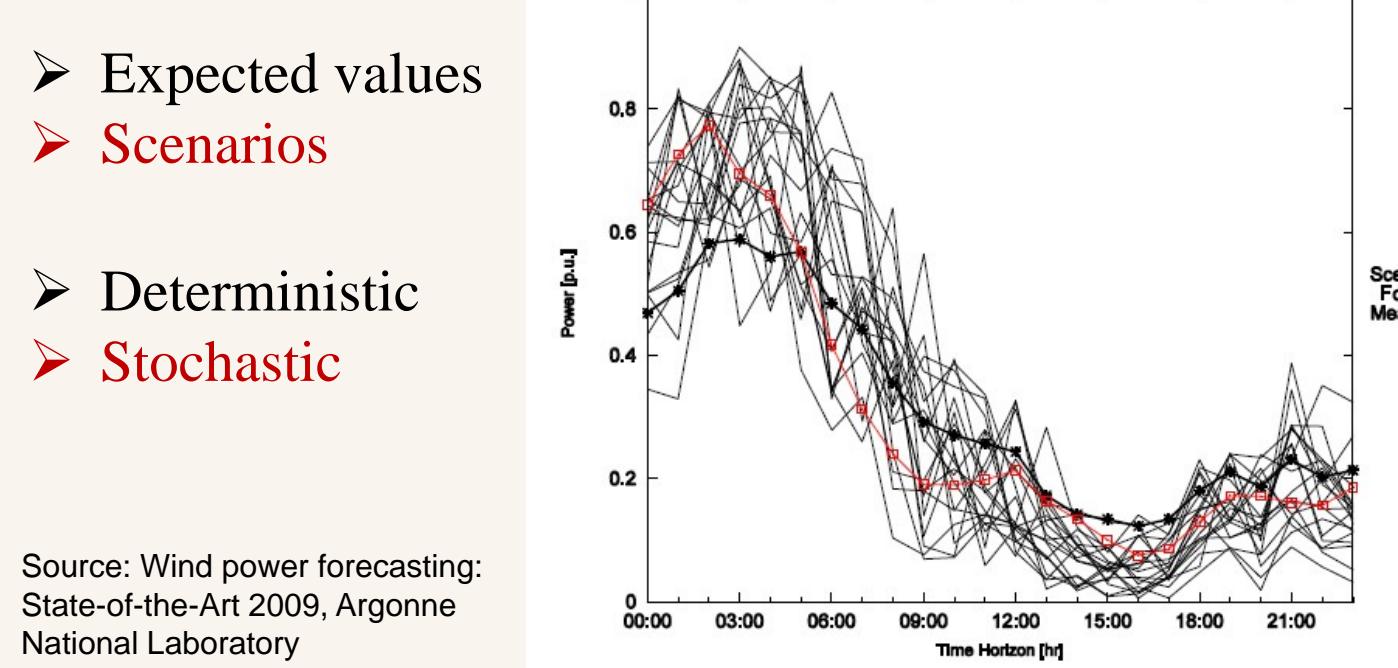


Decomposed Stochastic Model Predictive Control for Optimal Dispatch of Storage and Generation

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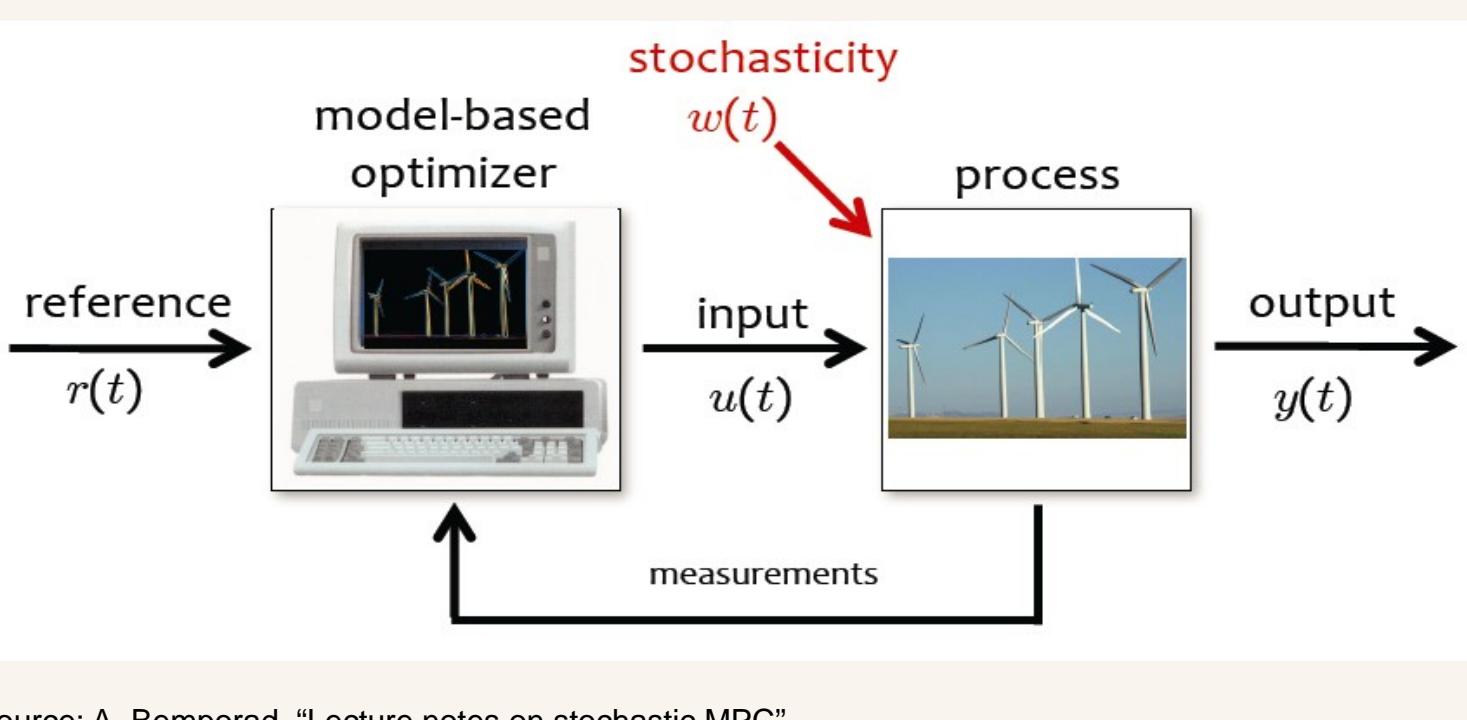
Introduction

- Motivation & Challenge
 - Uncertainties introduced by variable energy sources, e.g. wind and solar
 - Optimal operation of the emerging large scale energy storage devices
- Objective: safe and optimal scheduling of conventional generation and energy storage in near real time (e.g. 5min) under uncertainties to:
 - reduce ramp rates of generators
 - minimize total operation costs
- Key: uncertainty representation



SMPC Basics

- Stochastic model predictive control
 - Stochastic optimization
 - Model predictive control
- General concept



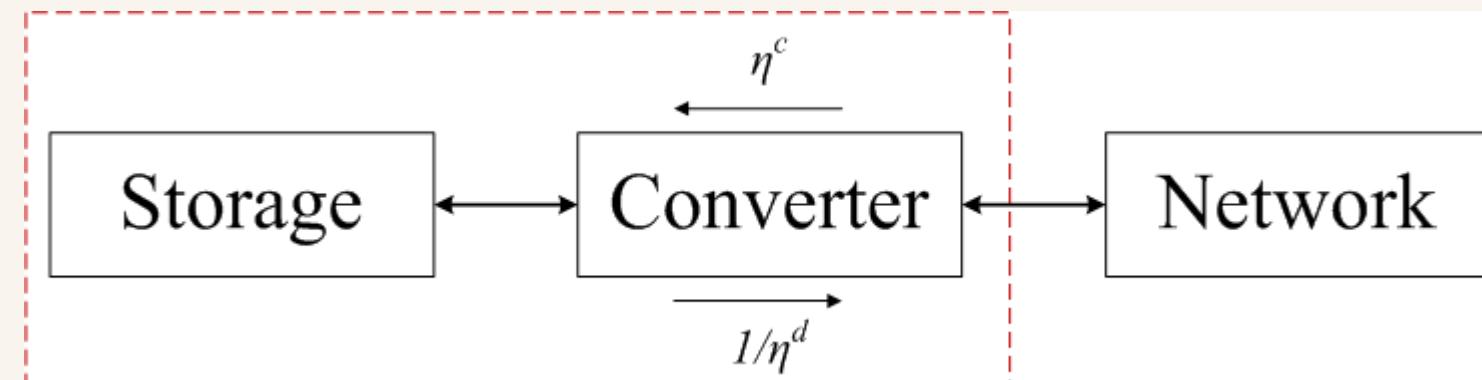
Source: A. Bemporad, "Lecture notes on stochastic MPC"

- Mathematical formulation

$$\begin{aligned} \min_{\mathbf{E}_w} \sum_{k=0}^{N-1} l[y(k+1) - r(k+1), u(k)] \\ x(k+1) = f(x(k), u(k), w(k)) \\ y(k) = g(x(k), u(k), w(k)) \\ \text{s.t.} \quad x^{\min} \leq x(k) \leq x^{\max} \\ y^{\min} \leq y(k) \leq y^{\max} \\ u^{\min} \leq u(k) \leq u^{\max} \end{aligned}$$

Modeling

- Energy storage & converter



- State-space model

$$E(k+1) = \alpha \cdot E(k) + T \cdot [\eta^c \cdot u^c(k) - (\eta^d)^{-1} \cdot u^d(k)]$$

$$u^c(k) \cdot u^d(k) = 0, \quad \forall k$$

$E(k)$: energy level at time k
 $u^c(k)$: charge power at time k
 $u^d(k)$: discharge power at time k
 α : related to standby losses
 T : time step size

- Conventional generator

$$p(k+1) = p(k) + u^g(k)$$

$p(k)$: generator output power at time k
 $u^g(k)$: increment in power output level

- Power network: DC power flow model

Formulation

- Two-stage SMPC problem

$$\begin{aligned} \min_{x^s(k), u^s(k)} \sum_{s \in \mathcal{N}} \pi^s \left[\sum_{k \in \mathcal{T}} l_k(x^s(k), u^s(k)) + l_{n_H}(x^s(n_H)) \right] \\ \text{s.t.} \quad x^s(k+1) = Ax^s(k) + Bu^s(k) \quad \forall s \in \mathcal{N}, k \in \mathcal{T} \quad (1a) \\ x^{\min} \leq x^s(k+1) \leq x^{\max} \quad \forall s \in \mathcal{N}, k \in \mathcal{T} \quad (1b) \\ u^{\min} \leq u^s(k) \leq u^{\max} \quad \forall s \in \mathcal{N}, k \in \mathcal{T} \quad (1c) \\ h(x^s(k), u^s(k), r^s(k), d^s(k)) \leq 0 \quad \forall s \in \mathcal{N}, k \in \mathcal{T} \quad (1d) \\ u^i(0) = u^j(0) \quad \forall i, j \in \mathcal{N} \quad (1e) \end{aligned}$$

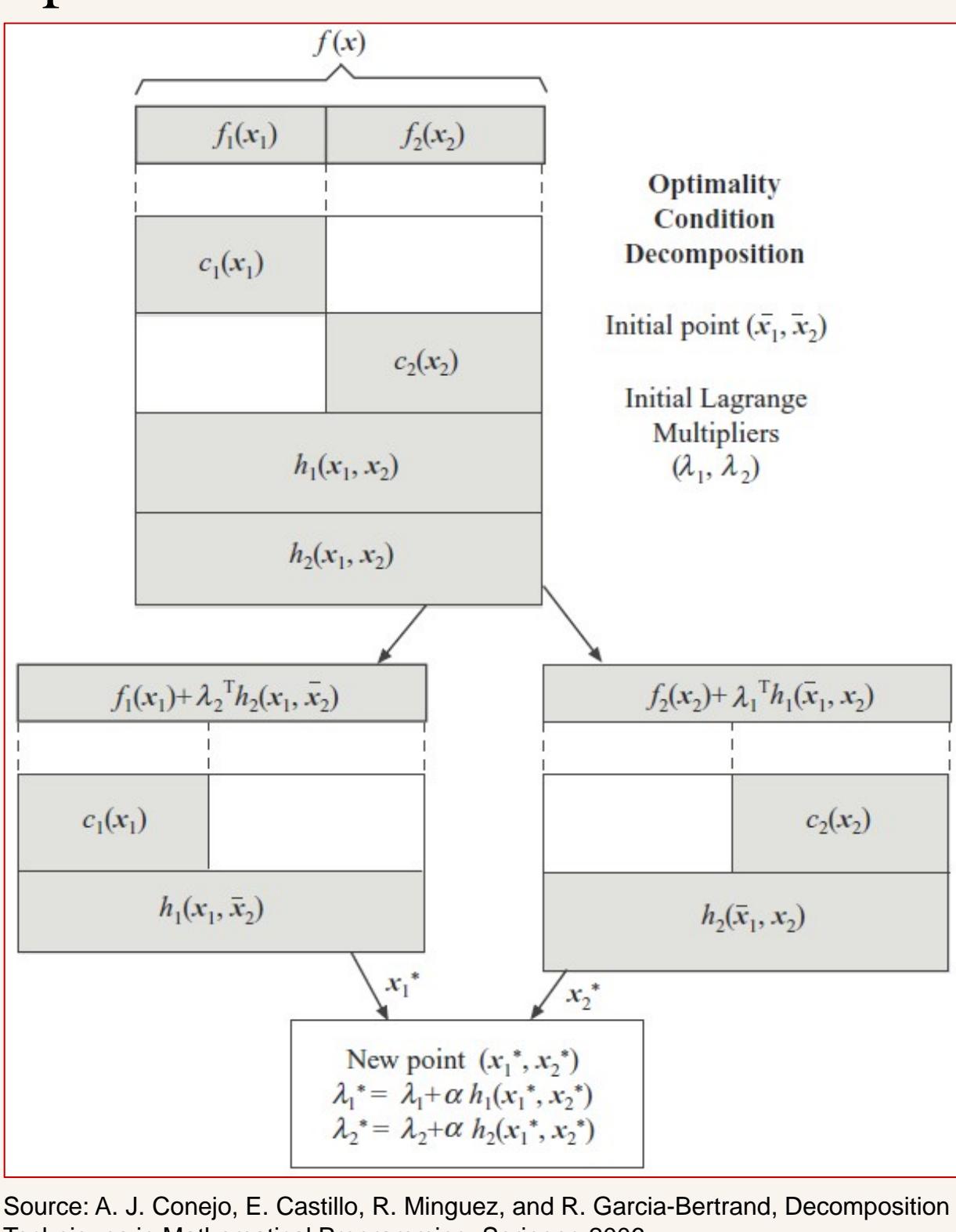
\mathcal{N} : set of all scenarios, $\mathcal{N} \triangleq \{1, \dots, N\}$,
 \mathcal{T} : set of the receding horizon, $\mathcal{T} \triangleq \{0, \dots, n_H - 1\}$,
 π^s : probability associated with Scenario s ,
 $x^s(k)$: storage energy levels and generator output levels,
 $u^s(k)$: control input for storages and generators,
 $r^s(k)$: power output of variable generation in Scenario s ,
 $d^s(k)$: demand at time k in Scenario s .

- Objective function

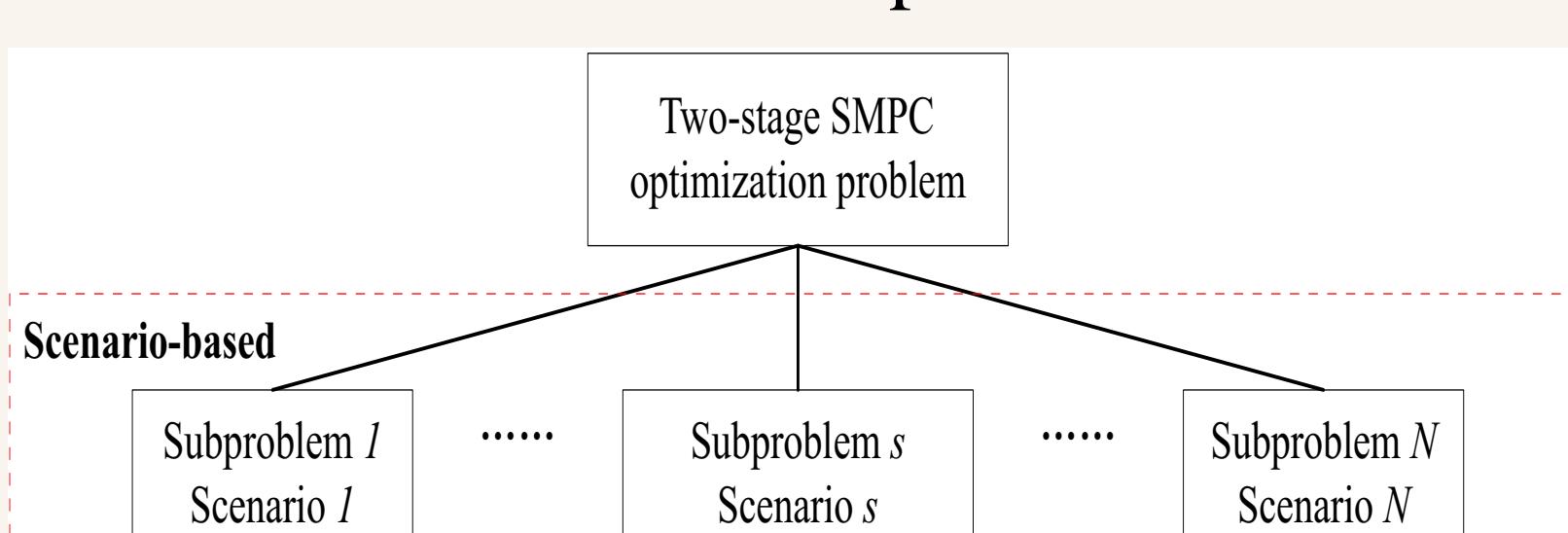
- Generator production cost
- Generator ramping cost
- Cost for storage conversion losses
- Nonanticipativity constraints in (1e)

OCD-based Solution Approach

- Graphical illustration of OCD



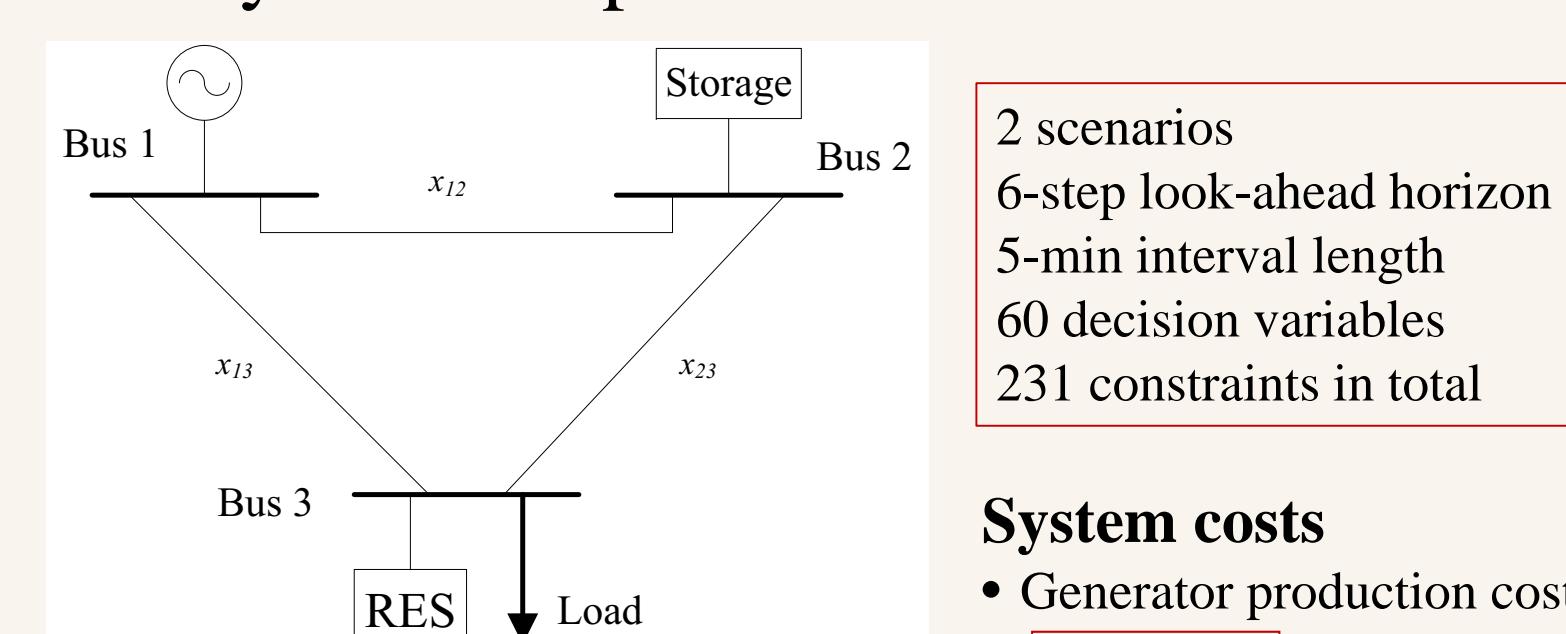
- Scenario-based decomposition



- Complicating constraints → (1e)
- Algorithm
 - Initialize all decision variables and Lagrangian multipliers;
 - Solve subproblems in parallel;
 - Update values of decision variables and multipliers obtained in Step 2;
 - If stopping criteria are fulfilled, stop. Else, go to Step 2).

Preliminary Simulation

- Consider an SMPC at a specific time step
- Test system setup



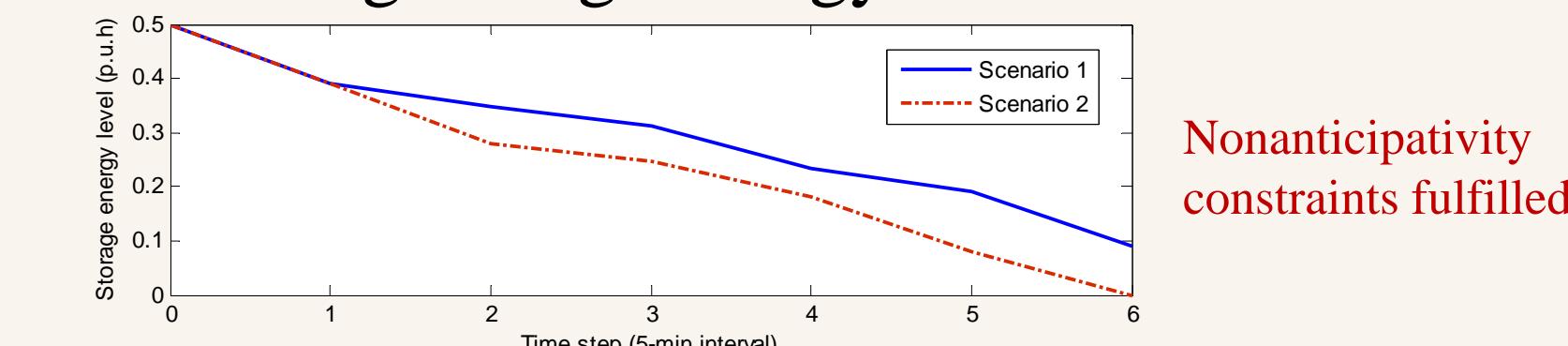
System costs

- Generator production cost $p^2(k) + 2p(k)$
- Generator ramping cost $10 \cdot (u^s(k))^2$
- Cost for conversion losses $T \cdot [(1 - \eta^c)u^c(k) + (\eta^d - 1)u^d(k)]$

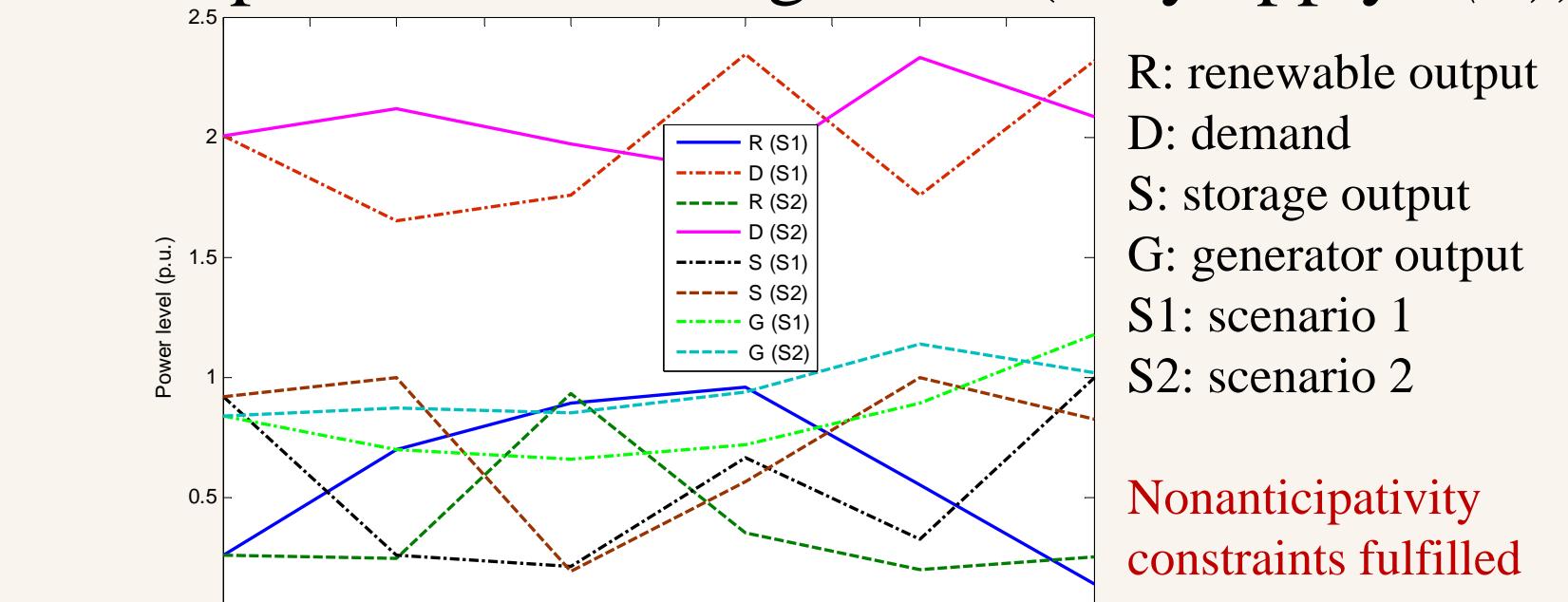
- System constraints

$$\begin{aligned} -1.5 \leq \text{line flow} \leq 1.5 \text{ p.u.} \\ 0.5 \leq p(k) \leq 2 \text{ p.u.}, -0.5 \leq u^s(k) \leq 0.5 \text{ p.u.} \\ 0 \leq E(k) \leq 1 \text{ p.u.h.}, 0 \leq u^c(k), u^d(k) \leq 1 \text{ p.u.} \end{aligned}$$

- Yielding storage energy level



- Optimal scheduling result (only apply $u(0)$)



- Convergence

